

# Modelling Water Scrubbing Biogas Based Technology

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# Why do we need a model?

- Description of real life situations
- Tool to help design and operate a system
- Provide predictions on how a system will behave under different conditions
- “Everything should be made as simple as possible, but not simpler”- Albert Einstein

# Modelling Approach

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graph TD; A[Modelling Approach] --> B[Equilibrium Based Models]; A --> C[Rate Based Models];
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## Equilibrium Based Models

- Empirical design
- HETP and HTU/NTU

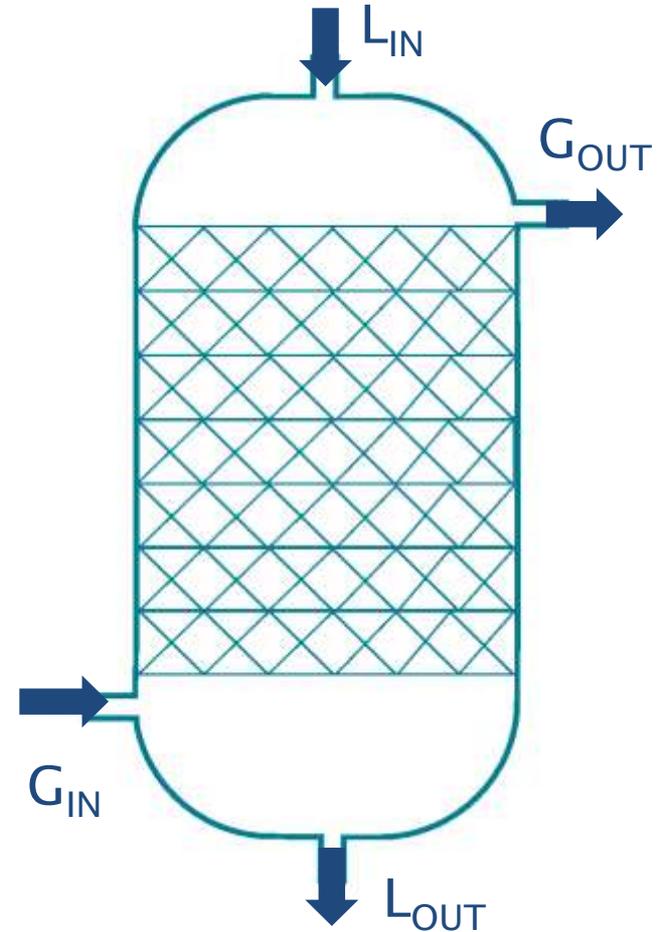
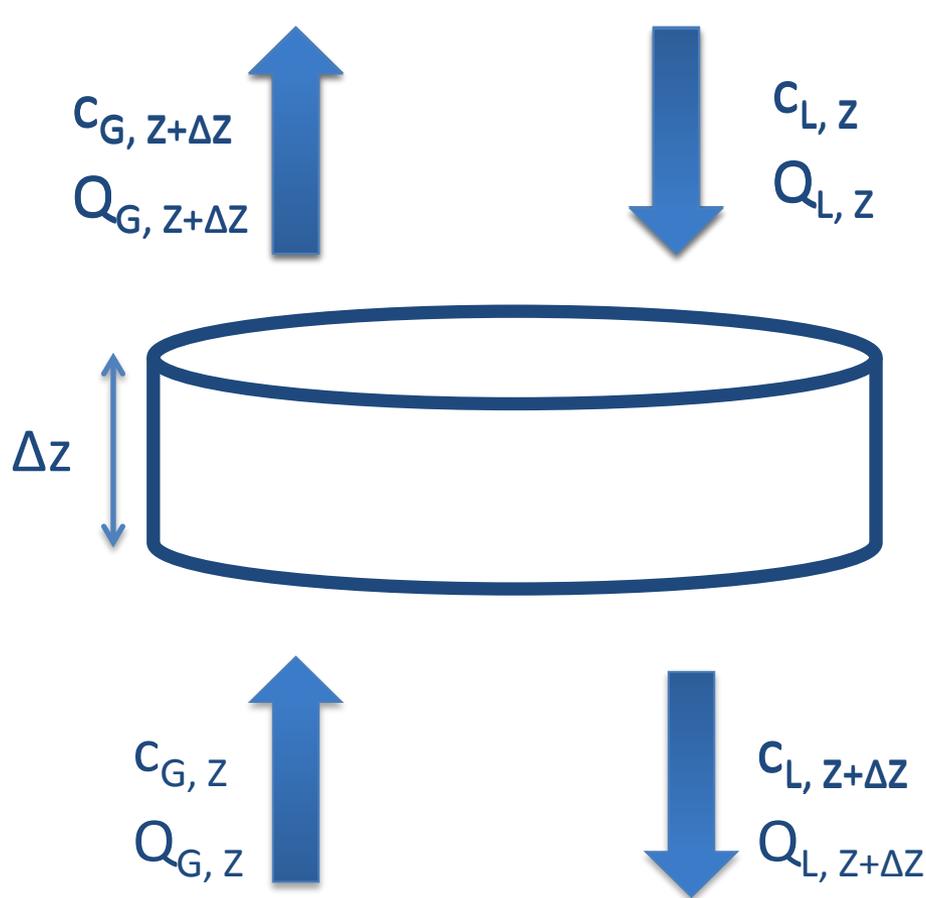
## Rate Based Models

- 1D, 2D or 3D
- Steady state or dynamic model
- CFD

# Modelling Assumptions

- Well mixed system with negligible directional concentration gradients
- Ideal Gas Law and ideal liquid flow
- Isothermal reactor
- Chemical reaction
- Which species should mass transfer consider
- Mass transfer liquid or gas side dominant?

# Model Derivation



# Plug Flow Reactor

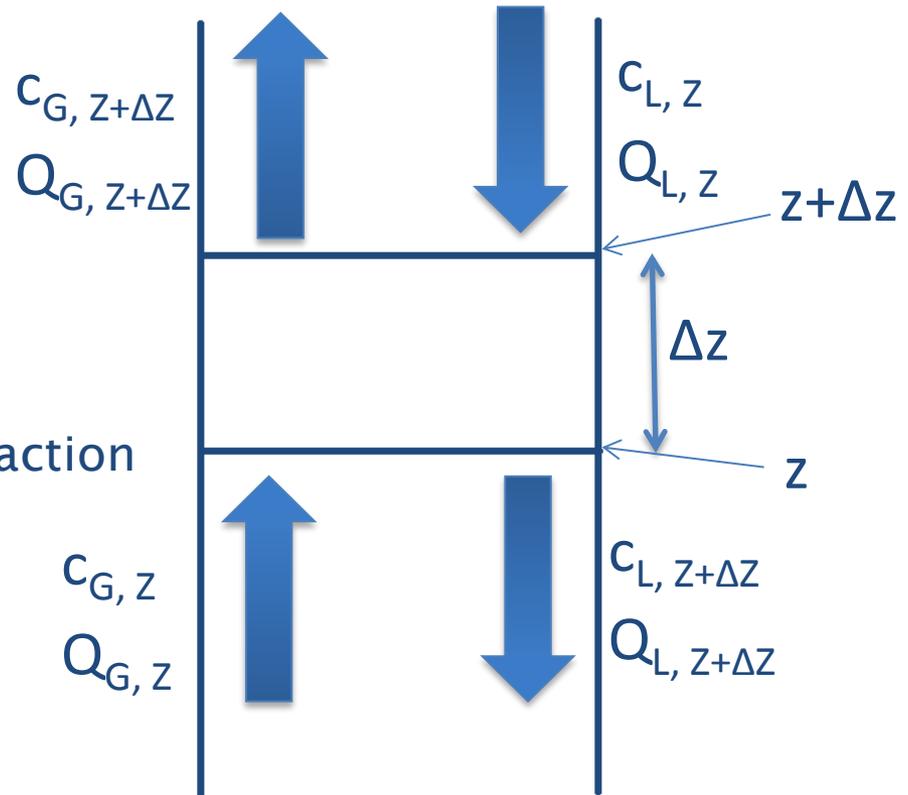
- Mass Balance:

$$\frac{\partial c_A}{\partial t} = Qc_A(z) - Qc_A(z + \Delta z) - r_A$$

Accumulation = input - output - reaction

$$\frac{\partial c_A}{\partial t} = -\frac{\partial(uc_A)}{\partial z} + r_A$$

- No axial mixing
- Perfect radial mixing



# Axial Dispersion Model

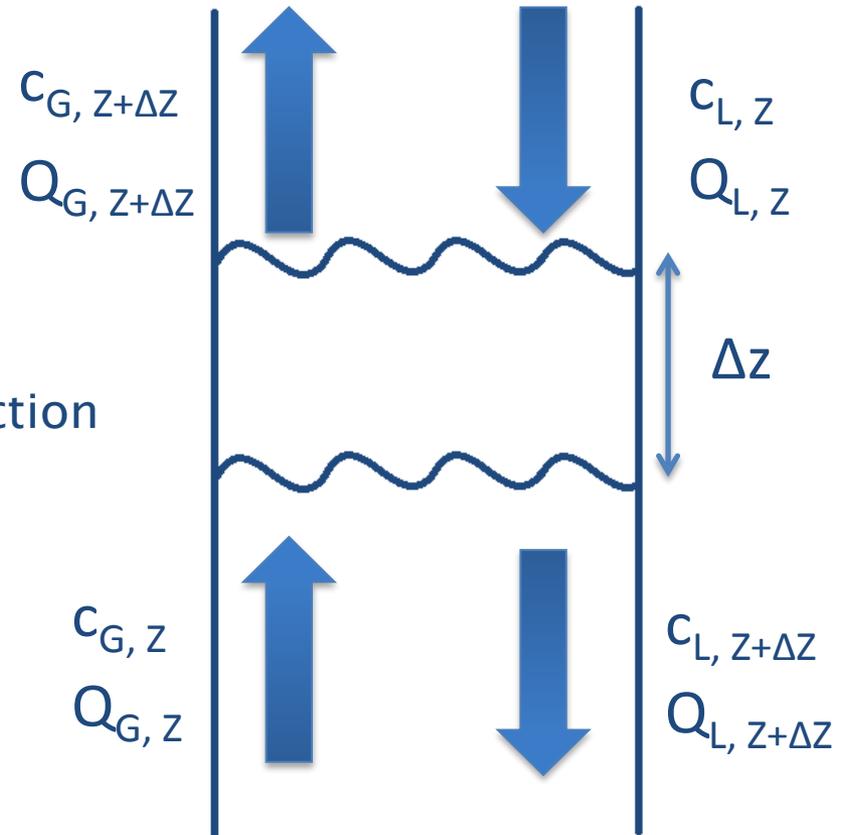
- Mass Balance:

$$\frac{\partial c_A}{\partial t} = D_A \frac{\partial^2 c_A}{\partial z^2} - \frac{\partial(uc_A)}{\partial z} - r_A$$

Accumulation = input - output - reaction

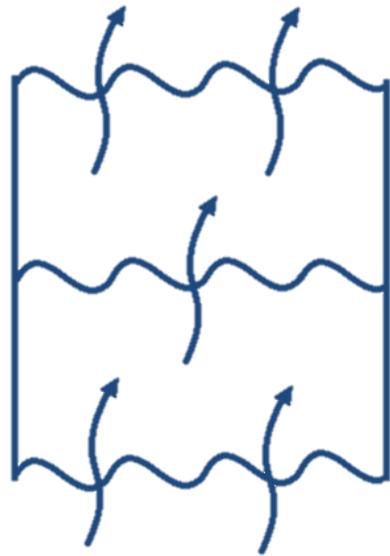
- Considers back mixing
- Peclet number

$$Pe = \frac{Lu}{D_A}$$

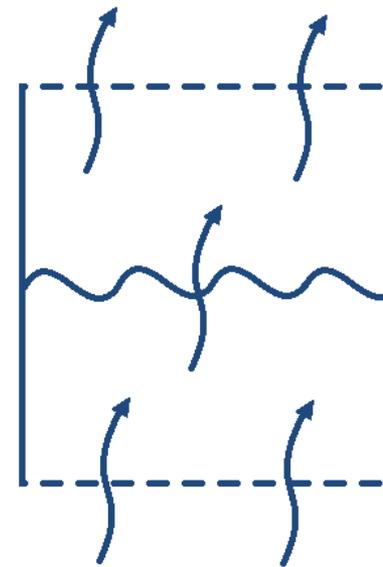


# Boundary Conditions

Open - Open



Closed - Closed

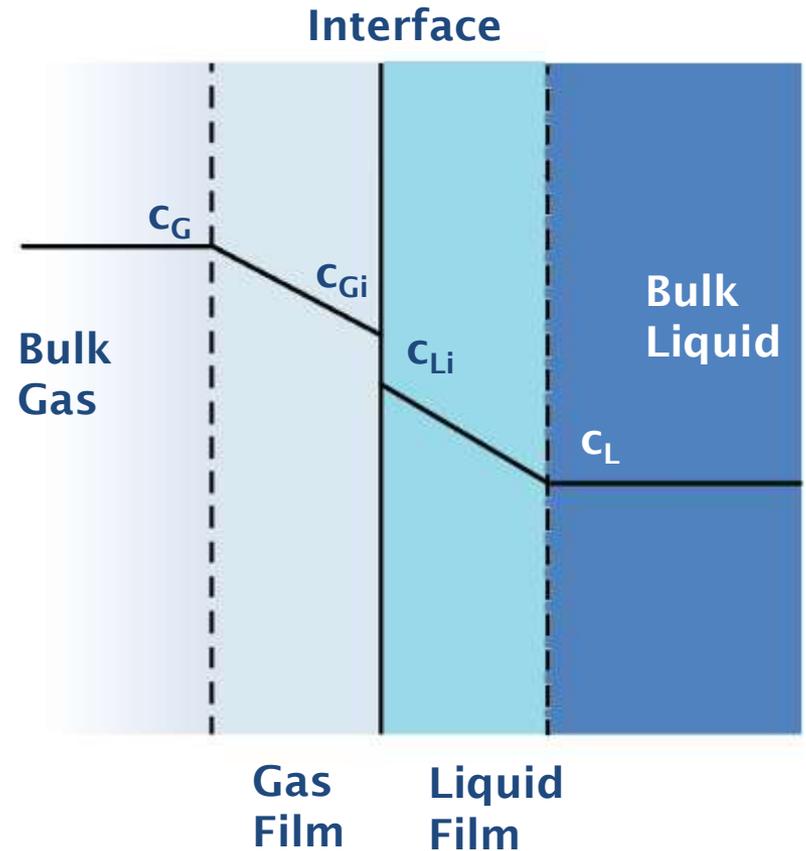


# Mass Transfer Theory

- Two - Film Theory

$$k_L = \frac{D_L}{\delta f}$$

- Film thickness
- Proportional to diffusion coefficient
- $N_A = k_L(c_G - c_{Gi})$

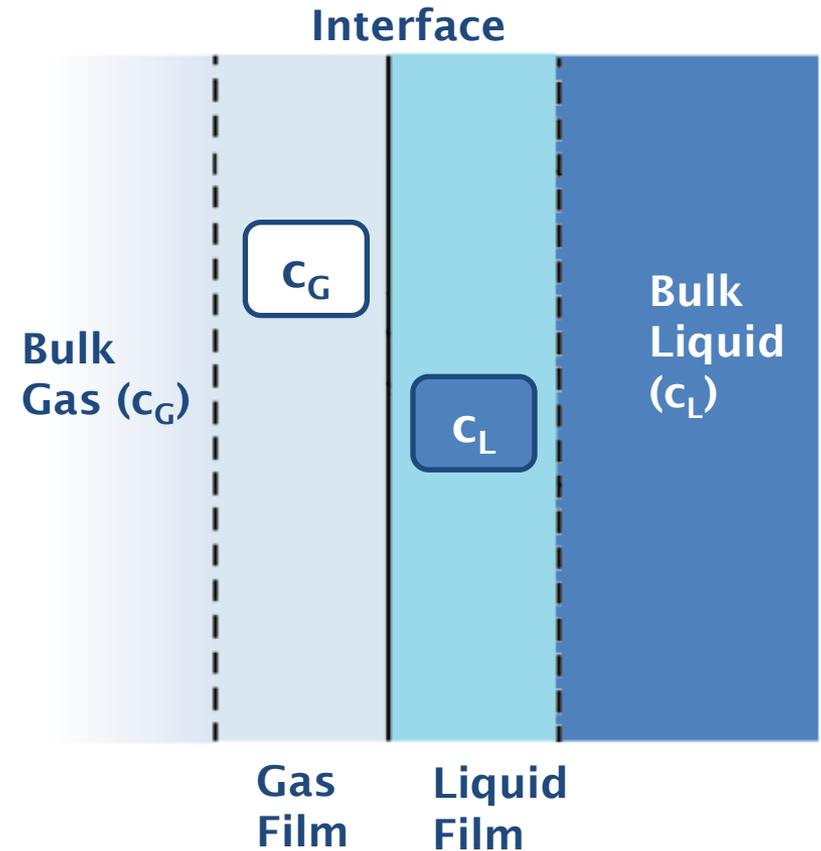


# Mass Transfer Theory

- Surface Renewal Theory

$$k_L = \sqrt{\frac{D_L}{t}}$$

- Contact time 'packets' in contact with interface
- Proportional to square root of diffusion coefficient



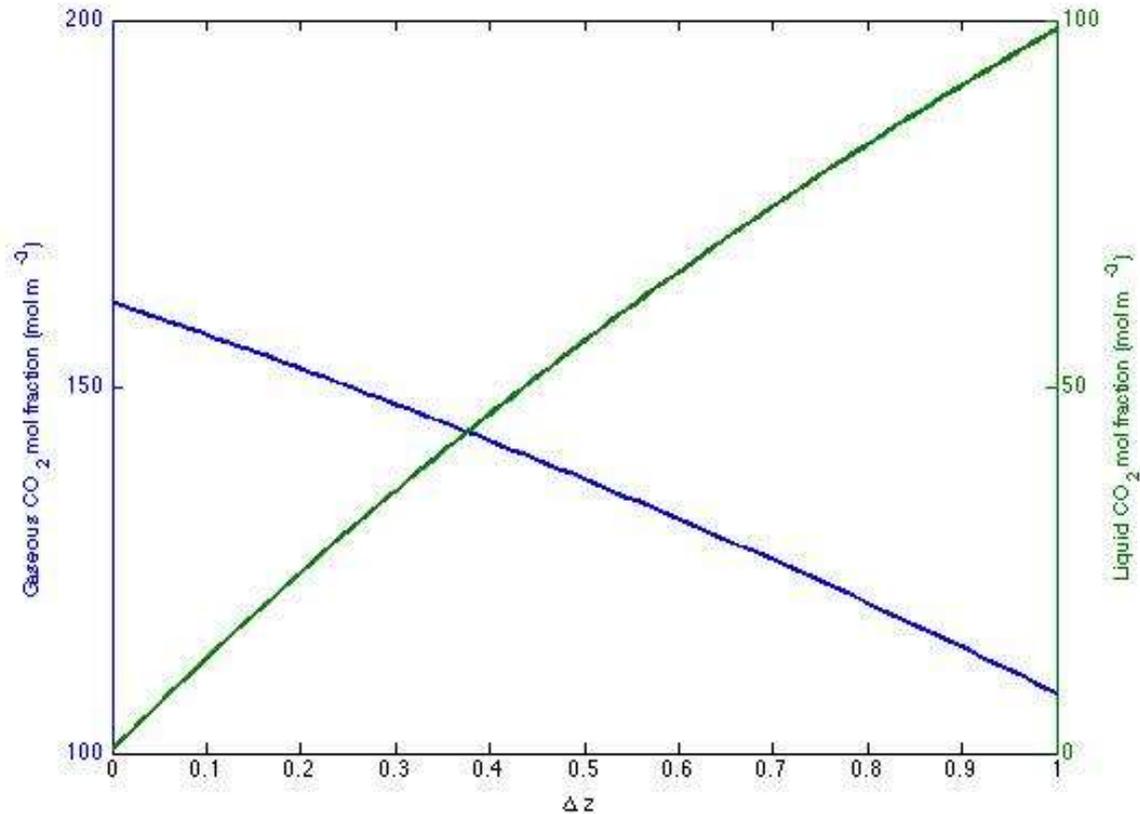
# Empirical Correlations

- Henry's Law
- Mass transfer coefficients
- Interfacial area
- Pressure drop
- Gas/ liquid holdup

# Finite Difference

- Numerical solution to ode and pde's.
- Explicit or implicit schemes
- Discretisation techniques
  - Upwind scheme:  $\frac{dc}{dz} = \left( \frac{c_{i+1} - c_i}{\Delta z} \right)$
- Multiphase counter-current flow
  - Gauss Seidel iteration

# Finite Difference



# Summary

- Simple models often out perform more detailed models
- Assumptions need to be taken with care

Thank you  
for listening